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SIMULATION OF CONTROL SYSTEM OF THE CHEMICAL-TECHNOLOGICAL PROCESSES

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ABSTRACT
In this work is consider study and analysis of dynamic system for simulation of the technological process under uncertainty and complexity. To study and simulate a complicated technology process we carry out for consideration the technology of the process of roasting in fluidized bed furnaces of polymetallic sulphide ores. The choice is justified by the fact that, operation line producing of polymetallic sulphide ores represents a complex process, is characterized by a big number of transient processes, presence of process variables and deviations from technical regimes. To study process characteristics of any system functioning by means of mathematical methods the process should be formalized. This means, that adequate mathematical model needs to be developed. The choice of mathematical model depends a lot upon the features of the object and its controllability as well as of technological scheme and complexity of processes. Chemical engineering processes are complicated physical and chemical systems. Substance flows, which are part of these systems, are, as a rule, multicomponent. Therefore, for the purpose of study and qualitative control over chemical-engineering processes it is essential to apply the method of mathematic simulation, based on system analysis strategy, analysis of its structure, mathematical formulation development and evaluation of unknown parameters. Controllability means that such system attribute as having control actions, which make it possible to transfer the system from a pre-set initial state to the required condition during finite quantum of time. Therefore, the developed mathematical model of the process or control object should be controllable and stability.


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Introduction. It is widely known that most of the practical systems operate with some degree of parametric uncertainty that can be a result of poorly known parameters of controlled plants or unpredictable changes of their values in the process of operation [1]. Therefore, robust stability can be viewed as one of the outstanding issues in control theory, which is also of a great practical interest. In general, the concept can be used to define the range of parameter variations that keep the system within stability boundaries. These boundaries are defined with respect to uncertain parameters of the controlled plant and can be affected by the settings of a control system. Known methods of control system design for objects with parametric uncertainty are usually based on determination of robust stability of systems with a given structure and with linear control laws or inertia-free (relay) characteristics [2].

They are usually not suitable for designing control systems with wide range of robust stability when the range of parametric uncertainty or parametric drift is significant. Therefore, developing novel
approaches to designing such systems is highly desirable. The results reported in [1, p.43] are obtained for dynamic systems that describe self-organizing processes in physical chemical and biological systems. The models of these systems are presented in the form of structurally-stable mappings based on catastrophe theory and they can be used as universal models of development and self-organization in nature [3]. Therefore, it is of great interest to consider great uncertainty of such systems and develop an automatic control system in the class of structurally stable mappings that uses the mathematical models reflecting complex behavior of the system with many possible stable solutions [2, 4].

In this paper, we address the issues of modeling the robust control systems for dynamic linear objects with uncertain parameters. Special attention is paid to the selection of a control law in the class of structurally stable mappings with one control factor [5] that allows maximizing the range of robust stability and improves characteristics of the system.

Materials and Methods

To have an object-orientated and effective technological process implemented, it should be controlled. This means, that in the process of engineering object functioning it is essential to have continuous influence on operating members, so as to provide achievement of the required single result, in spite of external disturbances.

In other words, when saying system controllability, we understand such system attribute as having control actions, which make it possible to transfer the system from a pre-set initial state to the required condition during finite quantum of time [6, 7].

Therefore, the developed mathematical model of the process or control object should be controllable. With this objection in mind let us consider our control object mathematical model and examine its controllability [8, 9].

Determination and Analysis Modelling Methods for Process

When simulating metallurgical processes and objects the most adequate approach is to choose structural approach for mathematical model development. In this respect, for simulating sulphurisation process we will consider molecular approach (as one of structural approaches). Metallurgical processes and objects are described on this level as an aggregate of physical and chemical phenomena, particularly as an aggregate of chemical reactions [10].

The process of roasting in fluidized bed furnaces of polymetallic sulphide ores represents a complicated chemical-and-technological process, including different stages of raw material (sulfurization) chemical changes. The yielded product quality depends upon the valuable component recovery percent in the end product. That is why it is assumed justified to develop mathematical model based on reactions chemical kinetics. Chemical kinetics is a science about chemical reactions proceeding in time behaviour and mechanism of these reactions. The main parameter here is some component formation rate. In metallurgy when modelling intricate chemical processes, normally, they are broken into separate stages of technological processes. Seeing on that, we suggest considering modelling the main stages of sulfurization from metal concentrate, control over these stages is one of the critical targets.

The processing method of concentrate of polymetallic sulphide ores of with sulfurization usage enables to extract metal from a multiplex poly metallic raw material into commercial metal. This method of sulphide extraction includes the following operations:
- sulfurization (oxidation) of metal concentrate;
- metal pulp leaching and dressing;
- extraction and re-extraction of sulphide;
- primary metal settlement;
- sulphide melting.

Based on the experience and this technology research it is determined, that main stages influencing the technological process and end product grade are sulfurization, and leaching. It means, further technology of sulphide oxidation depends upon the control over these main stages and upon how they proceed.

Design and Analysis of Control System for the Process of Roasting in Fluidized Bed Furnaces of Polymetallic Sulphide Ores

As we discussed above, the mathematical model of chemical reactions in this type of processes is described by mass balance equation of reagents \( A \) (metal) \( \oplus B \) (oxidation reagent), considering the complicated nature of the process, with the presence of diffusion and mass transfer. Therefore, in this case
the task of control is: to maintain components concentrations $C_A$ и $C_B$ as closer to specified ones $C_{A_{sp}}$ and $C_{B_{sp}}$ (required), changing concentrations of reagents $A$ и $B$, i.e., $C_{A_{11}}$ and $C_{B_{11}}$.

For design the control system for considering process, we simplify the equations, introducing relative coordinates and to can write the follow expressions:

$$d_1 = (k_1 * V)/F \quad \text{and} \quad d_3 = (k_3 * V)/F$$

(3)

where: $d_1$ - a concentrate of the first component in reactions $d_2$ - a concentrate of the second component in reactions.

$$t = (t' * F)/V$$

(4)

where: $t$ – period (time) needed for oxidation process of the metals.

$$x_1 = \frac{c_A}{C_{Aran}} \quad \text{and} \quad x_2 = \frac{c_B}{C_{Aran}}$$

(5)

$$u_1 = \frac{c_{A_{11}}}{C_{Aran}} \quad \text{and} \quad u_2 = \frac{c_{B_{11}}}{C_{Aran}}$$

(6)

where: $C_{Aran}$ - some chosen at random concentration value $C_A$ $d_1, d_3$ - coefficients for corresponding steps.

Then, after changing variables and parameters, the designing control system of our equations in these coordinates will give by:

$$\frac{dx_1}{dt} = -(1 + d_1) * x_1 + u_1; \quad x_1(0) = x_{10}$$

(7)

$$\frac{dx_2}{dt} = d_1 * x_1 - (1 + d_3) * x_2 + u_2; \quad x_{12}(0) = x_{20}$$

(8)

Study of Controllability and Stability of the Control System of Process: First Task

In this case the control target of regulating is defined this way: it is essential to maintain output coming concentrations $x_1$ и $x_2$ on specified levels, changing incoming concentrations $u_1$ и $u_2$.

Let us put the control system equation in vector-matrix form:

$$\frac{d}{dt} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -(1 + d_1) & 0 \\ d_1 & -(1 + d_3) \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} * u$$

(9)

$$\begin{bmatrix} x_1(0) \\ x_2(0) \end{bmatrix} = \begin{bmatrix} x_{10} \\ x_{20} \end{bmatrix} \quad \text{and} \quad x_{10} = 0, \quad x_{20} = 0$$

(10)

$$y(t) = [1 \quad 1] * \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \quad \text{and} \quad u(t) = [u_1 \quad u_2]$$

(11)

Once the model under consideration is rectilinear, it can be represented as an equation system in space of states (in the time domain). In standard form the system is given by:

$$A = \begin{bmatrix} -(1 + d_1) & 0 \\ d_1 & -(1 + d_3) \end{bmatrix}$$

(12)

$$B = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad C = [1 \quad 1] \quad \text{and} \quad D=0$$

(13)

Analysis of Controllability for Control System of Process

It is very important, when we are design a control system, to know, that this system have controllability [13]. The system is controllability, if it has such control as a $u(t)$, which can transfer a control system from her initial state $x_0$ to any state $x_f$ within final time.

Therefore, for current systems with matrixes $A$ и $B$ the controllability conditions are what control system will be full controllability, when rang of matrix of controllability $Lc$ equal $n (Lc = n)$, where:

$$Lc = [B : A * B : A^2 * B : \cdots : A^{n-1} * B]$$

(14)
In our case, to examine system controllability we make a controllability matrix for our case of the process.

Respectively controllability matrix \( L \) is given by:

\[
L = \begin{bmatrix}
1 & 0 & \vdots & -(1 + d_1) & 0 \\
0 & 0 & \ddots & 0 & -(1 + d_3)
\end{bmatrix}
\] (15)

In this case, controllability matrix rank \( L \) is also equal to two \((n=2)\), and this ensures the process controllability with one control action, though the quality of control will worsen. Thus, we can say, that our designed control system for the tellurium oxidation process in common case can be controllable, when we take a right regulation unit for keeping given regimes of technological process.

**Results and Discussion**

In the real technological processes and situations, we don’t have a possibility to control the both of parameters and variables. Therefore, it is need to analysis and to study the other condition for control system. It is the stability conditions for control plant, that is stronger than construability of the system.

The stability condition is in that, all of instability modes and eigenvectors of control system can be made stability by regulation impact in the closed-loop system.

Let us consider a case of control system of oxidation process of polymetallic sulphide ores for the linear regulator with constant coefficients, which are given in state space by expression:

\[
u(t) = -K \times y(t)
\] (16)

where: \( K \) – is \((m*n)\) matrix of closed loop system.

System (16) with this regulator can be show in follow form:

\[
\frac{dx}{dt} = (A - B \times K) \times x
\] (17)

It is following from above form, that stability of the system can be in that case, when we can to choose a matrix of closed loop system \( K \). In this way, all of eigenvectors of the matrix \((A-B*K)\) have negative real numbers.

If it is a case with control regulation by out coming:

\[
u(t) = -K \times x(t)
\] (18)

then a system will be given in the next form:

\[
\frac{dx}{dt} = (A - B \times K \times C) \times x
\] (19)

In this case stability is proved by choosing of such matrix \( K \), when a real eigenvector of matrix \((A-K*B*C)\) will be negative.

**Numerical Experiment Simulation of the Control System of Technological process**

The designed control system for technological process of roasting in fluidized bed furnaces of polymetallic sulphide ores and its controllable can be demonstrated by numerical simulations using computer software and modern technology of programming.

Let us consider this model, using actual example of technological process, having modelled it in MATLAB and Simulink. Assuming, that system parameters have the follow values (Table 1) (as example):

<table>
<thead>
<tr>
<th>Number of Experiments</th>
<th>Values of Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameters</td>
<td>k</td>
</tr>
<tr>
<td>1</td>
<td>k1=1</td>
</tr>
<tr>
<td>2</td>
<td>k2=2</td>
</tr>
</tbody>
</table>

Here the \( A \) is a concentrate of polymetallic sulphide ores and \( B \) is the concentration of oxidation reagent.
Let us to write our mathematical model is in the form of equation for state space:

$$\frac{dx}{dt} = A \cdot x + B \cdot u$$

$$y = C \cdot x$$ \hspace{1cm} (27)

Then, we can write the system function as a expression below:

$$F = [- (1+D1) \cdot x1 + u1; \ D1 \cdot x1 - (1+D2) \cdot x2 + u2 ]$$ \hspace{1cm} (28)

In this case, matrices of $A$ and $B$ will be written in the form of:

$$A = \begin{bmatrix} -4 & 0 \\ 3 & -2 \end{bmatrix} \quad B = \begin{bmatrix} 1 \\ 0 \end{bmatrix} \quad C = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \quad D = 0$$ \hspace{1cm} (29)

The model of the process of roasting in fluidized bed furnaces of polymetallic sulphide ores and the controller are set in such a way that, in the linearized form, the following parameters of the system are used in five different numerical simulations using Matlab (Table 2). Having made numerical experiments in Matlab, we get the following results and diagrams (Fig.1.-Fig.2):

![Fig.1](image1)

**Fig.1. Numerical simulation results: Experiment 1-2**

The waveforms presented in Fig.1 show stable performance for a different set of parameters and converge to equilibrium points.

![Fig.2](image2)

**Fig.2. Numerical simulation results: Experiment 3-4**

a) $k1=1 \quad k2=2$  

b) $k1=1 \quad k2=-2$

**Fig.1. Numerical simulation results: Experiment 1-2**

**Fig.2. Numerical simulation results: Experiment 3-4**

a) $k1=2 \quad k2=-3 \quad k3=5$  

b) $k1=2 \quad k2=3 \quad k3=5$
The this set of parameters results in an asymptotically stable system whose convergence process is shown in Fig. 2.

The waveforms in Fig. 1 and Fig. 2 are of particular interest, since they demonstrate stability. The results presented above illustrate that it is possible for the system to converge to an equilibrium point even if dynamics of the controlled process suddenly changes.

**Numerical Experiment Simulation of the Control System of the Technological Process**

The designed control system for real technological process of tellurium oxidation and its controllable can be demonstrated by numerical simulations using computer software and modern technology of programming.

Let us consider this model for second case, using actual example of technological process, having modelled it in Matlab and Simulink.

The pursued numerical experiments are given below (Table 2).

**Table 2. Values of parameters for numerical experiments**

<table>
<thead>
<tr>
<th>Number of Experiments</th>
<th>Value of Parameters nad Equations</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>N</td>
</tr>
<tr>
<td>a)</td>
<td>3</td>
</tr>
<tr>
<td>b)</td>
<td>1</td>
</tr>
</tbody>
</table>

Thus, for the second model the waveforms in these are of particular interest, since they demonstrate stability. The results presented above illustrate that it is possible for the system to converge to an equilibrium point even if dynamics of the controlled process suddenly changes. Though in practice, it is not always possible to control simultaneously all the parameters, and variables.

In the real technological processes and situations we don’t have a possibility to control the both of parameters and variables. Therefore, it is need to analysis and to study the other condition for control system with modelling of technological processes. It is the stability conditions for control plant, that is more stronger then controbility of the system.

In the case for the model 1, in practice it means, that, though both out coming concentrations of substances cannot be controlled only by changing B substance consumption. Concentration A is varying persistently and approaches to steady state irrespective of control. It means, the regulator for the system can be arranged, in spite of the fact, that the system is not fully controlled. Thus, control object is fully controlled towards controls A, but is not fully controlled towards control B.

**Conclusions.** Modern control methodologies are capable of increasing productivity of industrial cycles by means of automatic control, monitoring, and management systems. The components used for such control and monitoring tasks, including modern different sensors and devices, are usually tightly integrated with automatic systems that control the entire technological process. This approach facilitates the reduction of expenses used to service the main assets, allows increasing output productivity, reducing downtime, and finally to increase a controllability and stability of complex technological processes of industry.

In the same time for the purpose of study and qualitative control over chemical-engineering it is essential to apply the method of mathematic simulation, based on system analysis strategy, qualitative analysis of its structure, mathematical formulation development and evaluation of unknown parameters. Therefore, study of control systems and modeling of technological processes with the robust stability is one of the most important directions for enhancement, optimization and an intensification of the production facilities. The work in this part of research briefly describes an approach to assure robustness of a dynamic system. Its primary focus is on robust stability, not robust performance, in the presence of parameter variations and model uncertainties. Based on our analysis, the paper presents the conditions for converging to an equilibrium point and explains how to implement a controller to achieve robust stability for the technological process of roasting in fluidized bed furnaces of polymetallic sulphide ores.

In a number of applications where a system is characterized by nonlinear and time-varying behavior, the issue of stability and performance becomes very prominent. It is further complicated by
the fact that when a mathematical model is used as part of the control strategy, it is typically assumed to closely match the real process. However, the process-model mismatch often results in sub-standard performance or even stability issues. The latter can stem from improper controller gains that were chosen based on the assumed model of the controlled process.

The stability condition is that, all of unstability modes and eigenvectors of control system can be made stability by regulation impact in the closed-loop system. Considered a simulation of the technological process (process of roasting in fluidized bed furnaces of polymetallic sulphide ores), we found conditions for the stability of the system, the radius and transients. Thus, our robust stability study is specifying constraints on the control system parameters that preserve stability. These limits are determined by the region of stability in an uncertain and are selected. Using this methods of modeling and designing of control system and results of these studies we can design more effective control systems for the technological process and to obtain a product with high quality.

REFERENCES